EXPLAINING THE GEOMETRY OF SIMPLE MOLECULES USING MOLECULAR ORBITAL ENERGY-LEVEL DIAGRAMS BUILT BY USING SYMMETRY PRINCIPLES

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The built of qualitative energy-level molecular diagrams for different geometries of simple molecules allow to explain the preferred geometry. The diagrams are built using simple symmetry principles and explain, on basis of the number of nonbonding electrons, for example, why the molecule of water is bent and not linear and ammonia is pyramidal and not planar. This simple energy principle does not need to consider the Valence Shell Electron-Pair Repulsion theory (VSEPR theory) neither hybrid orbitals to explain the geometry of simple molecules. This discussion is more appropriate to inorganic chemistry courses where symmetry is a common topic.

Keywords: symmetry; group theory; molecular orbitals; molecular geometry

INTRODUCTION

The geometries of molecules like H₂O, NH₃, and CH₄ are usually explained, at undergraduate level, in general and inorganic chemistry courses, using the Valence Shell Electron-Pair Repulsion theory (VSEPR theory) and hybrid orbitals.¹,² In the case of the VSEPR the starting point is the Lewis structure of each compound. It is considered that electrons groups around the central atom will be as far as possible, producing the observed molecular geometry (linear for two electrons groups, triangular for three electrons groups, tetrahedral for four electrons groups, and so on). In the case of the molecules indicated above, all of them have four electron groups but some of these have lone pairs resulting in the H₂O bent, NH₃ pyramidal, and CH₄ tetrahedral geometry, as it is well known.

When using hybrid orbitals, the central atom in all these molecules is considered to use sp³ orbitals, which corresponds to the tetrahedral geometry. In this case some sp³ hybrid orbitals contain lone pair of electrons, resulting in the observed geometry for the cited molecules.

On the other hand, in the inorganic chemistry courses, when part of the time is dedicated to the application of symmetry to build the symmetry-adapted linear combinations of atomic orbitals, the stability of these molecules can be discussed more properly based on the molecular orbital energy-level diagrams for these molecules. Several inorganic chemistry textbooks present a very detailed molecular orbital energy-level diagrams for several simple molecules, for example, BeH₂, CO₂, and H₂O, justifying their geometries based on the occupancy of the molecular orbitals. However, as far we know, these textbooks do not present a discussion of what happen with the molecular energy if we consider a molecule with a different geometry.³,⁴ More specialized books on spectroscopy,⁵ present a discussion based on the change of the energy of molecular orbitals as the geometry of a molecule is gradually changed, for example, in the case of AH₃ species, changing from linear to bent geometry. This kind of discussion is based on qualitative Walsh diagrams.⁶⁻¹⁵ These Walsh diagrams describe how the energy of each molecular orbital changes as the molecular geometry is modified between two possibilities as, for example, linear and bent geometries. These gradual modifications on the energy of the molecular orbitals, however, in some cases, are not easy to forecast, making difficult the discussion in class.

Other works deal with the same subject we present in this article. Mulliken¹⁵ presents a discussion on NH₂ which considers this molecule in the geometries pyramidal and plane trigonal. However, he concludes that the pyramidal geometry is the preferred because of the mixing between s and pₓ nitrogen in bonding molecular orbitals of the pyramidal geometry. Baird¹⁶ presents a discussion on the geometries of several AX₃ molecules which is based on Walsh diagrams for the highest occupied molecular orbitals. Miller and Ellison¹⁷ also present Walsh diagrams calculated by a computational chemistry software for a series of AX₃ molecules, allowing discussing their geometries.

In this work we present the use of qualitative molecular orbital energy-level diagrams built from simple group theory principles of symmetry. However, differently from the articles cited above, our approach is based on the different occupancy of nonbonding molecular orbitals for each geometry of the molecule considered. This allows explain the preferred geometry of simple molecules without requiring the building of complete Walsh diagram. Our approach is simpler and is based mainly in the number of electrons on nonbonding molecular orbitals.

Symmetry is a common subject in inorganic chemistry courses (most commonly third or fourth semester or even later) and undergraduate students are very familiar with it. In this way, we have used the approach described below in the undergraduate inorganic chemistry course. We observed that the comparison of the energy-level molecular diagrams for different geometries of an specific molecule is a very significant application of symmetry and molecular orbital theory which gives a very strong support to more deep discussions of chemical bond based on molecular orbitals. The inclusion of this subject allowed show for the students a simple and direct application of symmetry and group theory on the very basic topic of molecular geometry together with the presentation of fundamental aspects of symmetry. This was a very significant improvement because we start to show an application of these principles earlier than before. Students, usually, are very anxious about where they will apply this knowledge, which is abstract, mathematical and spatial reasoning, being difficult for most part of the class. Before we have included this subject, the students need wait for the first application of symmetry until the discussing the electronic spectroscopy of transition metal complexes. As a consequence, we observed a very clear improvement in the number

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of the students which obtained higher grades in the questions related
with the basic principles of symmetry and group theory. We did not
apply a tool to measure this improvement but we estimated that
70 to 80% of the class have increased their comprehension level.

The starting point of this approach is the identification of the
irreducible representation of the atomic orbitals. After that, the energy
level diagram of the molecular orbitals is built, combining the atomic
orbitals of the same irreducible representation. Then, the molecular
orbitals are filled with the electrons using the aufbau principle.
Comparison of the number of electrons which occupy bonding,
antibonding, and nonbonding orbitals, at each different geometry of
the same molecule, allows explain its preferred molecular geometry.
In the following we consider that the reader knows the basic principles
of Group Theory applied to chemistry including symmetry operations
and the use of the Character Tables.4,6,18-22

THE WATER MOLECULE

This molecule has only two possible geometries indicated in
Figure 1: linear (D_{∞h}) and bent (C_{2v}). The convention for the coordinate
system and axis is the same used by Orchin and Jaffé,7 in which the
x axis is perpendicular to the plane of the molecule.

In the case of the bent geometry the molecule belongs to the point
group C_{2v} and its Character Table allows to identify the irreducible
representation of each oxygen (the central atom) atomic orbital based
on the last column indications (see Table 1). The 2s orbital has a
spherical symmetry and belongs to the totally symmetric irreducible
representation which is always the first to appear in any Character
Table, in this case A_{1}. The orbitals 2p_{x}, 2p_{y}, and 2p_{z}, belongs to B_{1},
B_{2}, and A_{1}, respectively. How these assignments are made, is shown
below for the symmetry operations of the group C_{2v}, as an example.
For other point groups this can be found in many textbooks which
show how to find the irreducible representation of the atomic orbitals
in a molecule.4,5,8-11

In the case of the C_{2}, \hat{C}_{2}^{(x)} and \hat{C}_{2}^{(y)} symmetry operators the
orbitals 2p_{x}, 2p_{y}, and 2p_{z} transform as shown in Figures 2, 3, and 4,
respectively.

To identify the irreducible representation for each orbital the result
of the application of the symmetry operator is taken as equal
to 1 if the orbital does not change and the result is -1 if the orbital
changes its signal. In this way, Table 1 shows the results and the
attribution of an irreducible representation for each oxygen atomic
orbital 2p_{x}, 2p_{y}, and 2p_{z}.

For the 1s atomic orbitals on each hydrogen (peripheral atoms),
indicated by s^{(H)}_{1} and s^{(H)}_{2}, they cannot be considered separately. As the
C_{2} symmetry operator exchange both 1s atomic orbitals, they must
be considered together using a two-dimensional matrix. In the case

Figure 1. The two possible geometries for the water molecule: linear (D_{∞h})
and bent (C_{2v}).

Figure 2. Results for the application of the \hat{C}_{2}^{(z)} operator (on the z axis), of
the (C_{2v}) point group, over the 2p_{x}, 2p_{y}, and 2p_{z} oxygen orbitals of the water
molecule.

Figure 3. Results for the application of the operator \hat{C}_{2}^{(x)}, of the (C_{2v}) point
group, over the 2p_{x}, 2p_{y}, and 2p_{z} oxygen orbitals of the water molecule.

Figure 4. Results for the application of the operator \hat{C}_{2}^{(y)}, of the (C_{2v}) point
group, over the 2p_{x}, 2p_{y}, and 2p_{z} oxygen orbitals of the water molecule.
Explaining the geometry of simple molecules

of the identity symmetry operation, the matrix representation of this operation can be indicated as

\[
\begin{bmatrix}
1 & 0 \\
0 & 1 \\
\end{bmatrix}
\]

This notation can be simplified considering that the first column and first line of the matrices refer to the sH1 atomic orbital and the second column and second line refer to the sH2 atomic orbital. In addition, the character or the trace of the matrix (\(\chi\), the sum of the main diagonal elements) is also indicated.

These results show that 1s atomic orbitals of the hydrogens produce a reducible representation which can be shown to be formed by the sum \(A_1 + B_2\) (see Table 2).

\[
\begin{array}{cccc}
\text{C}_2v & E & C_2 & \sigma_v^{(00)} & \sigma_v^{('00)} \\
A_1 & 1 & 1 & 1 & 1 \\
A_2 & 1 & 1 & -1 & -1 \\
B_1 & 1 & -1 & 1 & -1 \\
B_2 & 1 & -1 & -1 & 1 \\
\end{array}
\]

With this information we can set up the energy level diagram for the molecular orbitals of water (Figure 5), considering that only atomic orbitals of the same symmetry species can combine. The symmetry labels are written in lower case when indicating atomic and molecular orbitals. Note also that the 2p orbitals do not have any hydrogen orbitals to combine and because of this it stays as a \(b_1\) nonbonding molecular orbital which has the same energy level of the 2p atomic orbital.

Now, let us consider the possibility that the water molecule is linear. In this case the molecule will belong to the point group \(D_{sh}\) (Figure 1). Using the information on the last column of the Character Table (Table 3) we can assign the oxygen atomic orbitals to the following irreducible representations: 2s (\(\Sigma_g^*\), the totally symmetric representation), 2p, (\(\Sigma_u^*\)), and 2p, and 2p, together (\(\Pi_u\)).

In the case of the hydrogen 1s atomic orbitals, any \(C_2\) perpendicular to the principal axis (z) will exchange the hydrogens 1s orbitals in the atoms H1 and H2 and because of this they must be worked together using two dimensional matrices, as shown below.

These results show that 1s atomic orbitals of the hydrogens produce a reducible representation which can be shown to be formed by the sum \(A_1 + B_2\) (see Table 2).

\[
\begin{array}{cccc}
\text{C}_2v & E & C_2 & \sigma_v^{(00)} & \sigma_v^{('00)} \\
A_1 & 1 & 1 & 1 & 1 \\
A_2 & 1 & 1 & -1 & -1 \\
B_1 & 1 & -1 & 1 & -1 \\
B_2 & 1 & -1 & -1 & 1 \\
\end{array}
\]

With this information we can set up the energy level diagram for the molecular orbitals of water (Figure 5), considering that only atomic orbitals of the same symmetry species can combine. The symmetry labels are written in lower case when indicating atomic and molecular orbitals. Note also that the 2p, oxygen atomic orbital does not have any hydrogen orbitals to combine and because of this it stays as a \(b_1\) nonbonding molecular orbital which has the same energy level of the 2p, atomic orbital.

Table 1. Applying the \(C_{2v}\) symmetry operations to oxygen 2p, 2p, and 2p, atomic orbitals in the water molecule

<table>
<thead>
<tr>
<th>(\text{C}_{2v})</th>
<th>E</th>
<th>(C_2)</th>
<th>(\sigma_v^{(00)})</th>
<th>(\sigma_v^{('00)})</th>
</tr>
</thead>
<tbody>
<tr>
<td>A,</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>A,</td>
<td>1</td>
<td>1</td>
<td>-1</td>
<td>-1</td>
</tr>
<tr>
<td>B,</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>-1</td>
</tr>
<tr>
<td>B,</td>
<td>1</td>
<td>-1</td>
<td>-1</td>
<td>1</td>
</tr>
</tbody>
</table>

Table 2. Applying the \(C_{2v}\) symmetry operations to hydrogen 1s atomic orbitals in the water molecule

<table>
<thead>
<tr>
<th>(\text{C}_{2v})</th>
<th>E</th>
<th>(C_2)</th>
<th>(\sigma_v^{(00)})</th>
<th>(\sigma_v^{('00)})</th>
</tr>
</thead>
<tbody>
<tr>
<td>A,</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>A,</td>
<td>1</td>
<td>1</td>
<td>-1</td>
<td>-1</td>
</tr>
<tr>
<td>B,</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>-1</td>
</tr>
<tr>
<td>B,</td>
<td>1</td>
<td>-1</td>
<td>-1</td>
<td>1</td>
</tr>
</tbody>
</table>

\(\sigma_v^{(00)}\), \(\sigma_v^{('00)}\)

Figure 5. Qualitative molecular orbital energy-level diagram for water in the bent geometry (\(C_{2v}\))

\(\sigma_v^{(00)}\), \(\sigma_v^{('00)}\)

\(\sigma_v^{(00)}\), \(\sigma_v^{('00)}\)

These results show that 1s hydrogen orbitals (s\(H_1\), s\(H_2\)) produce a reducible representation which can be shown to be formed by \(\Sigma_g^* + \Sigma_u^*\) (see Table 3).

Using these results we can build the molecular orbital energy-level diagram for the water molecule in the linear geometry (\(D_{sh}\)), as is shown in Figure 6. Note that now the 2p, and 2p, oxygen atomic orbitals do not have any hydrogen orbitals with the same irreducible representation to combine and because of this they stay as a \(\pi_u\) nonbonding molecular orbital which has the same energy level of the 2p, and 2p, atomic orbitals.

Now, let us consider the possibility that the water molecule is linear. In this case the molecule will belong to the point group \(D_{sh}\) (Figure 1). Using the information on the last column of the Character Table (Table 3) we can assign the oxygen atomic orbitals to the following irreducible representations: 2s (\(\Sigma_g^*\), the totally symmetric representation), 2p, (\(\Sigma_u^*\)), and 2p, and 2p, together (\(\Pi_u\)).

In the case of the hydrogen 1s atomic orbitals, any \(C_2\) perpendicular to the principal axis (z) will exchange the hydrogens 1s orbitals in the atoms H1 and H2 and because of this they must be worked together using two dimensional matrices, as shown below.

These results show that 1s atomic orbitals of the hydrogens produce a reducible representation which can be shown to be formed by the sum \(A_1 + B_2\) (see Table 2).

\[
\begin{array}{cccc}
\text{C}_2 & E & C_2 & \sigma_v^{(00)} & \sigma_v^{('00)} \\
A_1 & 1 & 1 & 1 & 1 \\
A_2 & 1 & 1 & -1 & -1 \\
B_1 & 1 & -1 & 1 & -1 \\
B_2 & 1 & -1 & -1 & 1 \\
\end{array}
\]
Comparison between Figures 5 and 6 shows that in the linear geometry the water molecule has four electrons in two \( \pi_u \) nonbonding molecular orbitals, but in the bent geometry it has only two electrons in the \( b_1 \) nonbonding molecular orbital, being more stable in this geometry because it has more electrons in lower energy levels.

Clearly the reason for the bent geometry of the water molecule is that one of the \( \pi_u \) nonbonding molecular orbitals in the linear geometry becomes a bonding molecular orbital in the bent geometry, decreasing the energy of the molecule. The other \( \pi_u \) nonbonding molecular orbital stays as a \( b_1 \) nonbonding.

Some authors\(^{8,16,17}\) discuss in more detail the transformation of one set of orbitals in the other, as the geometry is changed from linear to bent, using the very well-known Walsh diagrams. This is a more detailed discussion which is necessary to explain the geometry of species with a lower number of electrons, like \( \text{BeH}_2 \), \( \text{CH}_2 \), \( \text{NH}_2 \), and \( \text{BH}_2^+ \), which are linear. In the case of water, it is necessary consider only the number of nonbonding electrons in both geometry.

It is worth to say that the conclusion that water is bent was obtained without consider the repulsion between the electrons pairs in the VSEPR theory or by the use of sp\(^3\) hybrid orbitals. In addition, the presence of three low energy peaks in the photoelectron spectrum of water is in a better agreement with the molecular orbital energy-level presented in Figure 5 than the presence of two sp\(^3\) nonbonding equivalent orbitals.\(^{23}\)

**THE AMMONIA MOLECULE**

The same approach used with the water molecule can be applied to explain the most stable geometry of other simple molecules. Let us now consider the \( \text{NH}_3 \) molecule in two different geometries: pyramidal (\( C_3v \)) and planar (\( D_3h \)) (Figure 7). Application of the same symmetry principles produces the results shown in Table 4.

![Figure 6. Qualitative molecular orbital energy-level diagram for water in the linear geometry (\( D_\infty h \))]()

![Figure 7. The two possible geometries for the ammonia molecule: pyramidal (\( C_3v \)) and planar (\( D_3h \))]()

**Table 3. Applying the \( D_3h \) symmetry operations to the hydrogen 1s atomic orbitals of the linear water molecule**

<table>
<thead>
<tr>
<th>( D_3h )</th>
<th>( \Sigma^+ )</th>
<th>( \Sigma^0 )</th>
<th>( \Pi^+ )</th>
<th>( \Delta^0 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>E</td>
<td>1</td>
<td>1</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>( 2C_z )</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>( \sigma_y )</td>
<td>1</td>
<td>1</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>( \sigma_z )</td>
<td>-1</td>
<td>-1</td>
<td>-2</td>
<td>-2</td>
</tr>
<tr>
<td>( \pi_y )</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

From these results we can say that both nitrogen 2s and 2p\(_z\) atomic orbitals belong to the irreducible representation \( A_1 \) and the orbitals 2p\(_x\) and 2p\(_y\) belongs to the irreducible representation \( E \). The three hydrogen 1s orbitals produce a reducible representation, which decomposes to \( A_1 + E \). With this information the qualitative molecular orbital energy-level diagram for \( \text{NH}_3 \) can be assembled as shown in Figure 8, as it is presented in many textbooks, without any nonbonding molecular orbital.

Let us now consider the \( \text{NH}_3 \) in the planar geometry (\( D_3h \)). Application of the principles of symmetry produces the results shown in Table 5, which indicates that the nitrogen 2s atomic orbital belongs to the irreducible representation \( A'_1 \) (totally symmetric),
Explaining the geometry of simple molecules

The three hydrogen 1s orbitals produce a reducible representation which is formed by \( A_1' + E' \). Using this information the molecular orbital energy-level diagram for \( \text{NH}_3 \) in the planar geometry (\( D_3h \)) can be built, as shown in Figure 9, which presents one electron pair in the \( a_2'' \) nonbonding molecular orbital.

Comparison between Figures 8 and 9 shows that \( \text{NH}_3 \) in the planar geometry has two electrons in the \( a_2'' \) nonbonding molecular orbitals, but in the pyramidal geometry it does not have electrons in nonbonding orbitals, being more stable in this geometry because it has more electrons in lower energy levels. Again the reason for the pyramidal geometry of the \( \text{NH}_3 \) molecule is the lower energy of the valence electrons in this geometry compared with the planar geometry, independent from the lower repulsion between the electrons pairs in the VSEPR theory or by the use of \( sp^3 \) hybrid orbitals.

THE METHANE MOLECULE

We can now consider the tetrahedral and planar geometry of methane, which belongs to the point groups \( T_d \) and \( D_{4h} \), respectively (Figure 10). Tables 6 and 7 and Figures 11 and 12 present the results for the application of symmetry concepts and the molecular orbital energy-level diagrams for both cases.

As can be seen from Figures 11 and 12 the methane in the planar geometry (\( D_{4h} \)) has one pair of electrons in the \( a_2'' \) nonbonding molecular orbital, but in the tetrahedral geometry there is no nonbonding molecular orbital occupied, which gives a lower energy for the \( T_d \) geometry than \( D_{4h} \) geometry.

BENT AND LINEAR THREE ATOM SPECIES WITH DOUBLE BONDS

In addition to these simple cases above, it is intriguing, for example, why is the ozone molecule bent and \( \text{CO}_2 \) linear? Table 8 shows several simple three atoms species and their electron valence...
counting. As can be seen, only sixteen electron species can be linear
\((D_{\infty h})\) as it was observed by other authors. To explain the geometries
of the species shown in Table 8 using molecular orbital energy-level
diagrams the situation now is more complex because instead of the
terminal hydrogen atoms we have now oxygen or nitrogen atoms.
It means that in addition to the \(s\) atomic orbitals, the terminal atoms
have three \(p\) orbitals, which makes more difficult to produce simple
molecular orbital energy-level diagrams. However, we can make a
simple analysis considering only the \(\pi\) frontier molecular, as it is
shown in Figure 13 for the \(CO_2\) molecule.

Table 7. Applying the \(D_{\infty h}\) symmetry operations to the atomic orbitals of the planar \(CH_4\) molecule

<table>
<thead>
<tr>
<th>(D_{\infty h})</th>
<th>E</th>
<th>(2C_4)</th>
<th>(C_2)</th>
<th>(2C_2')</th>
<th>(2C_2'')</th>
<th>(i)</th>
<th>(2S_4)</th>
<th>(\sigma_g)</th>
<th>(\sigma_u)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(A_{1g})</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>(A_{2g})</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>(B_{1g})</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>(B_{2g})</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>-1</td>
<td>-1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>(E_g)</td>
<td>2</td>
<td>0</td>
<td>-2</td>
<td>0</td>
<td>0</td>
<td>2</td>
<td>0</td>
<td>-2</td>
<td>0</td>
</tr>
<tr>
<td>(A_{1u})</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>-1</td>
<td>-1</td>
<td>-1</td>
<td>-1</td>
</tr>
<tr>
<td>(A_{2u})</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>-1</td>
<td>-1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>(B_{1u})</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>1</td>
<td>-1</td>
<td>-1</td>
<td>1</td>
</tr>
<tr>
<td>(B_{2u})</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>1</td>
<td>-1</td>
</tr>
<tr>
<td>(E_u)</td>
<td>2</td>
<td>0</td>
<td>-2</td>
<td>0</td>
<td>0</td>
<td>-2</td>
<td>0</td>
<td>2</td>
<td>0</td>
</tr>
</tbody>
</table>

\((x^m, y^m, z^m)\)

Table 8. Trinuclear \(AX_2\) species and their electron valence counting and
geometry

<table>
<thead>
<tr>
<th>Number of valence electrons</th>
<th>linear</th>
<th>bent</th>
</tr>
</thead>
<tbody>
<tr>
<td>16</td>
<td>(CO_2, N_i^+)</td>
<td>(NO_2^-)</td>
</tr>
<tr>
<td>17</td>
<td></td>
<td>(O_3, NO_2^-, SO_2)</td>
</tr>
<tr>
<td>18</td>
<td></td>
<td>(ClO_2^-)</td>
</tr>
<tr>
<td>19</td>
<td></td>
<td>(ClO_2^-)</td>
</tr>
</tbody>
</table>

Figure 11. Qualitative molecular orbital energy-level diagram for \(CH_4\) in the
tetrahedral geometry \((T_d)\)

Figure 12. Qualitative molecular orbital energy-level diagram for \(CH_4\) in the
planar geometry \((D_{\infty h})\)

Figure 13. Simplified molecular orbital energy-level diagram for \(CO_2\) \((16\) valence electrons) showing only the frontier \(\pi\) orbitals
As can be seen, the HOMO is a nonbonding $\pi$ molecular orbital and the LUMO is an empty $\pi$ antibonding molecular. For the species $N_2$, the molecular orbital energy-level diagram is similar, with the $\pi_2$ antibonding molecular orbital without electrons. However, for the species with more than 16 electrons in Table 8, the $\pi_2$ antibonding molecular orbital will be occupied and the linear geometry will have a higher energy than the bend geometry.

CONCLUSION

The use of qualitative molecular orbital energy-level diagrams build from simple principles of symmetry and group theory allows forecast the correct geometry between two possibilities for some simple molecules. The choice of the most stable geometry depends on the energy of all electrons in the molecule and their interactions. However, for the molecules $H_2O, NH_3, CH_4$ and some $AX_3$ species (X different of hydrogen), the decision between two geometric possibilities can be made only by counting the number of nonbonding electrons for each case.

This approach reinforces the importance of the knowledge of symmetry and molecular orbital principles and gives additional support to discussions of bonding and molecular geometry based in other principles as, for example, electron pair repulsion based in VSEPR theory or hybrid orbitals, which are more commonly teach in the beginning levels.

Molecules of the $AH_3$ type, with a lower number of electrons than water, like BeH$_2$, for example, cannot be discussed using the simple approach presented here. In this case and for many other species it is necessary use the more detailed Walsh diagrams, which consider the change in energy of the full set of valence shell molecular orbitals as the geometry is gradually changed between two possibilities. In addition, our approach does not allow a discussion of the angle in the case of $AH_3$ bent molecules or $AH_4$ pyramidal molecules. It is concerned only to the question between two extreme geometric possibilities like linear and bent ($AH_3$), planar or pyramidal ($AH_4$), etc. However, this simpler qualitative discussion has been able to improve the comprehension of the students in the symmetry concepts because this gives to them a strong answer to the question “why we need learn symmetry?”

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