LAÜE BACK-REFLECTION METHOD FOR CRYSTALLOGRAPHIC ORIENTATION OF A MARTENSITIC Cu-Zn-Al SINGLE CRYSTAL OF THE MONOCLINIC SYSTEM

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INTRODUCTION

The electrochemical behavior of copper-based alloys and their pure elements has been studied for many years by the authors in alkaline, salt and acid solutions\(^1\)\(^-\)\(^10\). These studies were conducted only with mono- or polyphasic polycrystalline alloys in the following metallurgical conditions: as cast, annealed, quenched or submitted to other heat treatments. Many results obtained for these metallic alloys were strongly influenced by copper, the majority element. For Cu-Al-Ag alloys, depending on the media and silver or aluminum concentration, the electrochemical behavior was influenced by silver\(^3\)\(^-\)\(^8\) or even controlled by aluminum\(^4\)\(^,\)\(^7\)\(^,\)\(^10\). The electrochemical response obtained with such polycrystalline materials is determined by the contribution of all crystalline planes present on the electrode surface and exposed to the solution. To go deeper on electrochemical studies of these copper-based alloys it was decided to study oriented single crystal of these materials.

Due to the difficulties to buy single crystals of copper-based alloys with a desired composition, a furnace previously described\(^11\) was modified and constructed\(^12\) in our laboratories to obtain single crystals based on the Bridgman’s method\(^13\). Our studies began with an easier crystallographic system, a single crystal \(\beta\) phase Cu-Zn-Al alloy, which belongs to the DO\(_3\) ordered structure. Single crystals were orientated in the (111), (110) and (100) crystallographic planes, using the Laüe back-reflection method\(^13\)\(^,\)\(^14\). Considering our interest in shape memory copper-based alloys\(^15\)\(^,\)\(^16\), simultaneously to the \(\beta\) phase Cu-Zn-Al preparation, martensitic Cu-Zn-Al single crystals were also obtained. Martensitic structures can also be originated from the \(\beta\) phase structure.

Starting from original \(\beta\) phase single crystal (body-centered cubic crystalline system) a martensitic phase can be obtained by cooling, and 24 martensite variants can be formed to self-accommodating. For instance, beginning with the plane present in the original phase, habitual planes found in the martensitic phase can be calculated. With stereographic projection 6 groups of these planes were found, each one with 4 variants or clusters around each plane. It is the case of the transformation from the original \(\beta\) phase (DO\(_3\)) to 18R, martensite (\(\beta'\)). Then each one of the 6 groups has 2 opposite directions itself and 2 equivalents because the variants are twinned, and 24 variants of martensitic structure single crystal are formed\(^10\)\(^,\)\(^17\). These can be described starting from orthorhombic unit cells and showing some distortion (monoclinic distortion) when compared to the perfect piling up of the original phase\(^17\). The martensitic transformation occurs by shearing, also called invariant tension of the plane. Its product generates invariant tension in the lattice, producing defects such as twinned plates, stack defects and/or dislocations\(^18\)\(^,\)\(^19\).

Metals and metallic alloys with these characteristics respond to the tension applied by sliding the plates and this process can be reversible; unlikely most of the metals do not show this transformation. A variant or a single way plates movement can be preferably formed, depending on the manner and form that martensitic materials are submitted to the tension stress. This fact is related to the sliding of the martensitic plates, which respond and interact with the applied tensile force used to obtain variants in a specific direction. This observation is a consequence of the lattice reversibility between the original phase and the martensitic one. The accommodation of the plates by means of non-diffusional displacements allows the conversion of one to another crystallographic system and vice-versa. This transformation can also be achieved by heating and cooling the Cu-Zn-Al alloy. This reversibility also characterizes the pseudo-elasticity of the material, which plays an important role in technological applications\(^20\).

The Cu-Zn-Al as well as other alloys, metals and materials are not always isotropic in their physical properties. An example is the module of elasticity (Young’s module) that changes with the crystallographic direction. Therefore, determining the orientation of a single crystal that will be submitted to some mechanical test to verify the relationship between a specific property and its crystallographic orientation is necessary.

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The Laüe back-reflection method can be used to orientate a single crystal to expose a specific plane at the surface. This method consists in analyzing a group of diffraction points (called spots) produced on the film, since the positions of these points are determined by the crystal orientation. It is used because a special preparation of the sample is not required and there is no thickness restriction, while the transmission method needs thin samples with small absorption.

In the Laüe back-reflection method, the sample begins to be orientated in relation to the film that has a square or rectangular form and a reference mark in one end of the film. For metallurgical purposes the shapes of single crystal samples are wires, stalks (sticks), foils or plates. In the Laüe back-reflection method, the planes of a zone are as beams that draw a conical surface, in which the axis is the zone axis and is tilted in relation to the incident beam forming a semi-vertex angle. Therefore, the diffraction on a Laüe back-reflection film comes as hyperboles or straight lines corresponding to the tilting of the zone axis.

To determine the plane normal coordinates from the measured coordinates of the diffraction spot on the film a graphical method was devised by Greninger, who developed a chart. When the center of the chart is placed in the center of the film the coordinates $\gamma$ and $\delta$ of the plane normal are directly provided by the position (in terms of x and y) of any corresponding diffraction and in any distance (D) between the sample and the film. The Greninger’s chart is graduated in intervals of 2 $^\circ$, drawing hyperbolic lines on a transparent sheet support and giving directly the angular coordinates of the plane normal causing the spot. Using the Greninger’s chart the spots in the Laüe’s film is transported to the Wulff net and the crystallographic orientation of the single crystal can be obtained. This method was used to described the crystallographic orientation of single crystals belonging to a cubic system and monoclinic system. However, the use of Laüe back-reflection method to orientate the single crystals belonging to the monoclinic system, such as minerals, metals or metallic alloys including copper-based martensitic samples, was not found in the literature.

No stereographic projection pattern for single crystals of the monoclinic system was found which could help the interpretation of the diffraction pattern or its orientation. So, the aim of this work is to determine the crystallographic orientation of a monoclinic system such as martensitic single crystals of Cu-Zn-Al alloy which were submitted to tension stress in order to reduce the number of variants. Considering that this structure shows some difficulty to be orientated due to the low symmetry of the crystalline system, details of the stereographic projection for this system and the manner to orientate single crystals in (010), (120) and (130) crystallographic planes are clearly described. These single crystals have been used for electrochemical studies. Therefore, this work can present an important contribution to the field and to many electrochemists who intend to study non-commercially available single crystals. Also, very simple and low cost equipments are needed.

EXPERIMENTAL

The Cu-Zn-Al alloy preparation

The Cu-23.95Zn-3.62(wt.%)Al alloy was prepared by placing pure copper, zinc and aluminum elements inside a quartz blister sealed under vacuum, and by melting in an inductance furnace at 1400 °C. The cylinder of the polycrystalline alloy obtained was cut in little pieces and put in another quartz blister sealed under vacuum. The blister was placed in a modified Bridgman’s furnace constructed in our laboratory and the material was slowly run through the longitudinal axis of the furnace where the alloy was remelted and the single crystal was obtained.

Crystal characterization and orientation

Initially, the single crystal was polished and etched with FeCl$_3$ alcoholic solution (5 g FeCl$_3$ + 30 cm$^3$ HCl concentrated + 30 cm$^3$ isomylic or isopentylic alcohol + 30 cm$^3$ ethyl alcohol + 5 cm$^3$ distilled water) for different times to reveal the presence of one or more than one crystal. Using optical microscope this sample was analyzed and many variants were observed, which made the crystal orientation almost impossible since any variant diffracts as a single crystal. To solve this problem the single crystal was stretched applying a tensile force of 8 t in the longitudinal direction of the cylinder (15 cm length) to reduce the number of variants from 24 to one, which was confirmed after repeating the etching on the stretched crystal followed by OM analysis.

Diffraction system for crystal orientation

A Rigaku X-ray generator, serial UX 10031, with a tube of copper was used for crystallographic studies. To reduce the exposure time the X-rays tubes must have an anti-cathode that produces high white radiation and operates close to 30 or 35 kV. Tubes of W, Mo or Ag are also appropriate. A Laüe camera with a collimator and goniometer with a large angular freedom degree (18 $^\circ$) in X and Y completed the diffraction system.

Crystal orientation

The sample was orientated in relation to the rectangular film supplied by Kodak (mammography film), in which a reference mark was made in one end of the film. Afterwards, the crystal was exposed to the X-ray beam (Cu white radiation) operating at 35 kV and 20 mA for 30 min. Then, the film was developed and fixed using appropriate solutions prepared in our laboratory.

The developed Laüe back-reflection film contains a great number of diffraction spots, which represent the planes that diffract the X-ray beam. The families of planes that were in the diffraction position are responsible for diffracting X-ray beams. Considering that the film is positioned 3 cm from the crystal and a film of 127 x 180 mm is used, all planes in the zone whose zone axis is disposed at angles higher than 35 $^\circ$ respect to the X-ray beam will produce spots on the film. The diffraction spots form hyperbolic curves which represent crystallographic zones. Some of these curves possess much more diffraction spots than others, indicating that they represent a larger population of planes of low Miller indices. In order to analyse a group of spots belonging to the same zone the Greninger’s chart can be used.

The Laüe back-reflection film was covered by a transparent sheet fixed on the film. The Greninger’s chart was placed on the center of the film which has a mark to identified the correct position to be interpreted. Afterwards, the coordinates of the diffraction spots were directly read on the chart and these coordinates were placed in a stereographic projection with the help of a Wulff net. It is extremely important to put the meridians in the position from West to East. From the points localized in the same meridian (zone), all zones and zone axis were found and the angles between the zone axis were measured. For a cubic system these values can be directly compared with those already published.

However, in the case of monoclinic system no zone axis and angles between the zone axis values were published. So, considering the parameters of the unit cell for the single crystal here studied,
the interplanar angles for a large number of planes were calculated using a software. The results were used to construct the stereographic projection in the [001] direction, since no projection pattern for helping the diffraction interpretation exists.

After many attempts the desired crystal orientation can be found and the crystal must be fixed in the goniometer to be polished or cut without losing the orientation. To fix the orientated crystal on the goniometer, resin was applied and left resting for 24 h to impede any movement of the Teflon piece and of the crystal during the polishing or cutting of the sample. The goniometer was inserted in a cylinder of stainless steel, 5 cm height and 5 cm inner diameter (5.8 cm outer diameter), with three teeth properly projected to make an angle of 90 degrees with the surface of the sandpaper. It allowed the sample to be polished in the same angle in which it was adjusted.

RESULTS AND DISCUSSION

Characterization of martensitic Cu-Zn-Al single crystal

The studied sample was obtained from a single crystal Cu-23.95Zn-3.62(wt.%)Al alloy, monoclinic system and martensitic structure prepared as described in the experimental section. The parameters of unit cell previously obtained are: a₀ = 4.420 Å, b₀ = 5.323 Å, c₀ = 38.313 Å, â = 88.68 °. The following equation has been used to get the crystal structure parameters after the reference (1):

\[ \frac{1}{d_{hkl}^2} = \frac{1}{\sin^2 \beta} \left( \frac{h^2}{a^2} + \frac{k^2 \sin^2 \beta}{b^2} + \frac{l^2}{c^2} - \frac{2hl \cos \beta}{ac} \right) \]

Thus, using the (hkl) index of the diffraction peaks, the equation can be solved for giving a, b, c and β cell parameters. A typical martensitic structure was observed (Figure 1).

Crystal orientation

For monoclinic systems as mentioned above, each crystal has its own stereographic projection. Then, a theoretical projection in the direction of (001) plane was made for the Cu-Zn-Al single crystal using the crystallographic data a, b and c and the β angle as shown in Figure 2.

Figure 3a shows the film obtained during the first exposure of the top of the sample to the X-ray beam. The single crystal diffraction spots were observed with some enlargement due to the tension present in the lattice. Interpretation of the film was practically impossible because no hyperboles (zones) of diffraction exist. As crystallographic principle, the diffraction spots of high intensity are diffractions of planes with low Miller indices. Then, the spot marked in Figure 3a was moved to the center of the film, generating the film of Figure 3b. Although this film did not show diffraction hyperboles two lines exist (traced zones, Figure 3b), each one joining three diffraction spots and making an angle of 88 ° to each other. This angle is the angle between the a and c spots (zones axes) of the stereographic projection shown in Figure 4. This value is almost the same mentioned above for the β angle (88.68 °). From Figure 4 it was not possible to find a spot for the b parameter that was simultaneously 90 ° in relation to spots for the a and c parameters. It means that no plane with low Miller index was found from this exposure of the top of the crystal.

Therefore, the longitudinal parts of the crystal were exposed to X-ray beam. After several attempts the film shown in Figure 5 was obtained. The Laüe diffractions are a characteristic of single crystals which represent defined spots resulting in two hyperboles (zones), one at the inferior and the other at the superior part of the film (Figure 5a). Also between the two hyperboles a straight line can be drawn (zone) containing four spots (the lines were drawn to the laüegram to facilitate the visualization). In this case, no orientated plane with low Miller index was found.

The difficulty present in this system is the low symmetry and also the possible existence of more than one martensitic variant. For monoclinic structure (low symmetry) submitted to stretch, it was expected to obtain a single crystal with few variants, close to an ideal structure with one variant. However, even if a single crystal with few variants is obtained, the difficulty to find the desired orientation is higher than for a single crystal having only one variant. This happens because there is always the possibility that the laüegram shows contribution of other variants. As a consequence, a small change
in the position of the sample to search the desired orientation allows the interference of a new variant, losing all the previous work. One can observe one variant in one field and eventually two in another observed field, which means the possibility of an influence of the second variant in the examined field. In this case, the Laüe diffraction is not similar to that for a material with high symmetry (for example, cubic system in which hyperboles are well defined, making it easier to access low Miller indices), but it is for a system with low symmetry, which can lead to high Miller indices.

When the marked spot of Figure 5a was moved to the center of the film, a new film was obtained (Figure 5b). Now, it is possible to note a certain symmetry when a diagonal line is traced starting from a spot marked with a circle in Figure 5b, passing through the center of the film, where the spot previously marked in Figure 5a is.

With the Greninger’s chart the spots present in Figure 5b were transferred to the Wulff net, as showed in Figure 6. Beginning from the zone axis, which coincides with the center of the film (O), the zone 1 was generated. This zone represents the maximum equatorial circle of the Wulff net itself. Zone 2 passes through three diffraction spots in Figure 6 and generates the zone axis represented by a. Zone 3 passes through two spots plus the spot in the center of the film and generates the zone axis represented by c.

For this monoclinic system, the angles between the lattice parameters are: 90 ° between a and b, 90 ° between b and c and 88.68 ° between a and c, called β angle. The β angle between a and c was 88 ° (Figure 6), which is close to the value between the a and c parameters. Now, it is necessary to find a spot that corresponds to the b parameter. This parameter must be positioned simultaneously 90 ° from a and c in order to satisfy the expected conditions for this monoclinic system. The b parameter shown in Figure 6 was found in the crossing of zones 2 and 3. As the spot b is shifted from the center of the film the following procedure is necessary to the indexation of the plane located in the center of the film. It was necessary to use the Wull net to find the angles from the center of the film (normal to the plane at the center) to the parameters a, b and c. The following values were obtained for these parameters: 69 °, 23 ° and 90 °, and they are called director angles for each parameter. Then, Hái’s parametric relationships were used to determine the index of the plane that corresponds to the orientation of this single crystal. Using Hái’s parametric relationship, the director angles $P_a$, $P_b$ and $P_c$ (69 °, 23 ° and 90 °) and the lattice parameters ($a_0 = 4.420 \, \text{Å}$, $b_0 = 5.323 \, \text{Å}$, $c_0 = 38.313 \, \text{Å}$) the following equation was found (Equation 2):

$$h : k : l = a_0 \cos P_a : b_0 \cos P_b : c_0 \cos P_c$$  \hspace{1cm} (2)

which allows to calculate and determine the index of the orientated crystallographic plane.

Introducing the values for $a_0$, $b_0$, $c_0$ and $P_a$, $P_b$ and $P_c$ in Equation 2 the following relationship is obtained:

$$h : k : l = 4.420 \cos 69 \, ^\circ : 5.323 \cos 23 \, ^\circ : 38.313 \cos 90 \, ^\circ$$

The index of the orientated crystallographic plane was

$$(h \, k \, l) = (1 \, 3 \, 0)$$

Thus, the orientation of martensitic Cu-Zn-Al single crystal submitted to tensile stress was determined.

In many cases it is difficult to decide which spot must be placed at the center of the film since the index of the plane which is diffracting is unkown. To solve this problem an artifice can be used: it consists in applying a filtered radiation. This kind of filter was chosen because it avoids the absorption of unwanted radiations such as Cu Kβ and others longer than 1.5418 angstrons wavelengths, allowing to pass only the Cu Kα radiation. (The use of filtered radiation does not correspond exactly to the Laüe method). So, the films of Figure 7 were obtained with a few spots. Therefore, the monochromatic

![Figure 4. Stereographic projection of the film of Figure 3b](image)

![Figure 5. Laüegram of the longitudinal part of the martensitic Cu-Zn-Al single crystal (a) and after moving the circled spot to the center of the film (b)](image)

![Figure 6. Stereographic projection of the film of Figure 5b](image)
wavelength imposes that a few planes are in position to diffract (Figure 7a). This procedure allows to measure the diffraction $\theta$ angle to obtain the $d(hkl)$ value and the $(hkl)$ of the diffracting plane. In fact an artifice was used to obtain the $\theta$ angle from only one wavelength radiation. Thus, it was possible to identify the $d(hkl)$ and $(hkl)$ of some spots. The $(hkl)$ for each spot was calculated using Equation 3, Bragg’s Equation 4 and the following parameters: the radiation wavelength $(1.54 \text{ Å})$; the distance $(D)$ between the crystal and the film; and the distance from the center of the film to the spot $(r)$.

\[
\tan(\theta) = \frac{r}{D} \tag{3}
\]
\[
\lambda = 2d \sin \theta \tag{4}
\]

where $\theta$ = the angle ($^\circ$); $\lambda$ = wavelength ($\text{Cu K}\alpha = 1.54 \text{ Å}$) and $d(hkl)$ = interplanar spacing.

Using the webpage “Crystal Planes Spacings and Interplanar angles.htm” and knowing the $d_{(hkl)}$ values calculated with Equations 3 and 4, the Miller index $(hkl)$ of the diffracting plane was found (Figure 7b).

\[
d_{(hkl)} = \frac{\lambda}{2 \sin \theta} = \frac{1.54 \text{ Å}}{2 \sin(19.67^\circ)} = 1.54 \text{ Å} \cdot \frac{1}{0.67} = 2.30 \text{ Å}
\]

This value $(2.30 \text{ Å})$ is the closest value to $2.28 \text{ Å}$, which corresponds to the $(120)$ plane. The lâiegram obtained after moving the circled spot (Figure 7b) to the center of the film is shown in Figure 8. In the next steps Figure 8 was compared with the theoretical projection (Figure 2): it was observed that the $(120)$ plane is $30^\circ$ from the $(010)$ plane, and both are located in the equatorial zone. As the goniometer does not allow the rotation of the crystal in the equatorial plane, it was manually rotated around its vertical axis and then the $(010)$ crystallographic plane was orientated. The $(010)$ direction coincides with the crystallographic axis of $b$ and is perpendicular to the $(010)$ plane. The $(010)$ direction is either a binary axis or it is contained in a symmetry plane, being the $(010)$ plane very important due to its low Miller index.

When the $(010)$ crystallographic plane was orientated the lâiegram of the martensitic Cu-Zn-Al single crystal submitted to tensile force was obtained and its spots were not well defined (Figure 9a). In Figure 9b the corresponding stereographic projection is shown. This orientation, from the crystallographic viewpoint, is important because it coincides with a binary symmetry axis or a plane, which is the only one observed in the $b$ direction for monoclinic systems ($abc$ and $\alpha = \gamma = 90^\circ$ and $\beta \neq 90^\circ$).

In Figure 7b the circled spot of the lâiegram corresponds to a $(hkl) = (120)$, as can be demonstrated by the calculation shown below. From Figure 7a, the distance $(r)$ between the center of the film and the corresponding circled spot (Figure 7b) is $2.45 \text{ cm}$, from eq. 3 the $\tan(2\theta) = 0.82$ and $\theta = 19.67^\circ$. From Equation 4 the following $d_{(120)}$ value is obtained:

\[
d_{(120)} = \frac{\lambda}{2 \sin \theta} = \frac{1.54 \text{ Å}}{2 \sin(19.67^\circ)} = 2.28 \text{ Å}
\]

The diffraction spots in the $(120)$ plane are well defined (Figure 8), while this is not for the $(010)$ plane (Figure 9a). It seems that a higher tension occurs more in the $(010)$ plane than in the $(120)$ one due to the stretching suffered by the $(010)$ plane when the sample was submitted to tension stress.
CONCLUSIONS

The possibility of orientation of a single crystal belonging to a low symmetry system, such as the monoclinic one, without the use of any sophisticated method or software was demonstrated. For martensitic single crystal Cu-Zn-Al alloy submitted to a tension of 8 t the following crystalllographic orientations were obtained: (010), (120) and (130).

The elongated spots in the laüegram indicated that the higher tension stress was applied in the [010] direction when compared to the [120] one causing a stretching in the (010) plane, i.e., the single crystal was deformed in the (010) set of planes.

SUPPLEMENTARY MATERIAL

Supplementary Material describes the Laüe Camera and goniometer and their use are in http://quimicanova.sbq.org.br, in PDF file.

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